

Solution

The value of the turns ratio is, $a = \frac{V_1}{V_2} = \frac{200}{400} = 0.5$

The value of the total resistance referred to the secondary is,

$$R_{02} = R_2 + \frac{R_1}{a^2} = 0.8 + \frac{0.3}{0.25} = 2 \Omega$$

The total reactance referred to the primary is,

$$X_{02} = X_2 + \frac{X_1}{a^2} = 1.6 + \frac{0.6}{0.25} = 4 \Omega$$

The no-load voltage is,

$$E_2 = (V_2 \cos \phi_2 + I_2 R_{02}) + j(V_2 \sin \phi_2 + I_2 X_{02})$$

$$E_2 = (400 \times 0.8 + 10 \times 2) + j(400 \times 0.6 + 40)$$

$$E_2 = 440.5 \angle 39.5^\circ \text{ V}$$

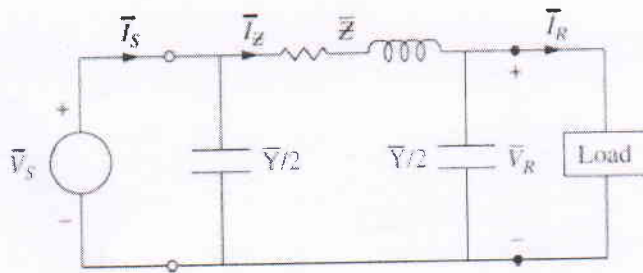
The voltage regulation can be determined as,

$$\text{Voltage regulation} = \frac{E_2 - V_2}{V_2} \times 100\%$$

$$\text{Voltage regulation} = \frac{440.5 - 400}{400} \times 100\% = 10\%$$

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(a) The nominal π circuit is shown below:



$$\begin{aligned} \text{The total line impedance } \bar{Z} &= (0.1826 + j0.784)100 = 18.26 + j78.4 \\ &= 80.5 \angle 76.89^\circ \Omega/\text{ph}. \end{aligned}$$

The line admittance for 100 mi is

$$\bar{Y} = \frac{1}{X_c} \angle 90^\circ = \frac{1}{\frac{185.5 \times 10^3}{100}} \angle 90^\circ = 0.5391 \times 10^{-3} \angle 90^\circ \text{ S/ph.}$$

$$(b) \bar{V}_R = \frac{230}{\sqrt{3}} \angle 0^\circ = 132.8 \angle 0^\circ \text{ kV}$$

$$\bar{I}_R = \frac{200 \times 10^3}{\sqrt{3}(230)} \angle 0^\circ = 502 \angle 0^\circ \text{ A } (\because \text{Unity Power Factor})$$

$$\begin{aligned} \bar{I}_Z &= \bar{I}_R + \bar{V}_R \left(\frac{\bar{Y}}{2} \right) = 502 \angle 0^\circ + (132,800 \angle 0^\circ)(0.27 \times 10^{-3} \angle 90^\circ) \\ &= 502 + j35.86 = 503.3 \angle 4.09^\circ \text{ A} \end{aligned}$$

$$\begin{aligned} \text{The sending end voltage } \bar{V}_S &= 132.8 \angle 0^\circ + (0.5033 \angle 4.09^\circ)(80.5 \angle 76.89^\circ) \\ &= 139.152 + j40.01 = 144.79 \angle 16.04^\circ \text{ kV} \end{aligned}$$

The line-to-line voltage magnitude at the sending end is $\sqrt{3}(144.79) = 250.784 \text{ kV}$

$$\begin{aligned} \bar{I}_S &= \bar{I}_Z + \bar{V}_S \left(\frac{\bar{Y}}{2} \right) = 502 + j35.86 + (144.79 \angle 16.04^\circ)(0.27 \angle 90^\circ) \\ &= 491.2 + j73.46 = 496.7 \angle 8.5^\circ \text{ A} \end{aligned}$$

$$\text{Sending end power } \bar{S}_{S(3\phi)} = 3(144.79)(0.4967) \angle 16.04^\circ - 8.5^\circ$$

$$\begin{aligned} \text{Sending end power } \bar{S}_{S(3\phi)} &= 3(144.79)(0.4967) \angle 16.04^\circ - 8.5^\circ \\ &= 213.88 + j28.31 \text{ MVA} \end{aligned}$$

$$\text{So } P_{S(3\phi)} = 213.88 \text{ MW}; Q_{S(3\phi)} = 28.31 \text{ MVAR}$$